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Application of Particle Swarm Optimization in Optimal Asset Allocation

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Authors' contributions

This work was carried out in collaboration among all authors. All authors read and approved the final manuscript.

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Short Communication

Abstract

Particle Swarm Optimization (PSO) is an effective tool for solving nonlinear, non-convex optimization problems, offering a quick and efficient way to identify rational asset allocations. In PSO, each particle represents a specific asset allocation and moves within the search space to optimize the defined criteria. Particles update their positions based on personal experience (individual best) and the collective experience of the swarm (global best), gradually converging toward an optimal solution.

Research on applying PSO to asset allocation demonstrates that this algorithm not only optimizes expected returns but also minimizes risk in investment portfolios. With its adaptability and computational speed, PSO can become a valuable tool for investors in formulating flexible and effective asset allocation strategies in a volatile financial environment.

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1 Introduction

In modern finance, optimal asset allocation is a fundamental problem that investors face in constructing portfolios to balance risk and reward. As financial markets become increasingly complex and volatile, finding an efficient way to distribute assets across various investment options, such as stocks, bonds, and real estate, becomes crucial to achieving desired returns within an acceptable risk framework. Traditional asset allocation methods, while effective in certain scenarios, often struggle with the large, complex search spaces and nonlinearity inherent in financial markets, which makes finding global optima both time-consuming and computationally challenging.

Particle Swarm Optimization (PSO), a bio-inspired optimization technique modeled on the social behaviors observed in flocks of birds or schools of fish, presents a promising solution for these challenges. Developed to solve complex, non-convex, and nonlinear optimization problems, PSO has demonstrated substantial success in various fields due to its adaptability, simplicity, and efficiency. The algorithm operates by generating a "swarm" of candidate solutions, referred to as particles, that explore the search space based on both personal and collective experiences. This approach enables PSO to achieve faster convergence toward optimal solutions compared to many traditional optimization techniques (Hosein, 1990).

In the context of optimal asset allocation, PSO offers a powerful means to dynamically adjust investment portfolios by optimizing the allocation across different asset classes. Each particle in the PSO represents a possible asset allocation scheme, which it updates iteratively in search of the optimal balance between maximizing expected returns and minimizing risk. The collective intelligence of the swarm allows the algorithm to avoid local optima and explore the search space more comprehensively, leading to a more robust portfolio composition (Lloyd & Witsenhausen, 1986; Ihsan et al., 2021; Abadi et al., 2015).

This paper explores the application of PSO in asset allocation, focusing on its ability to manage complex tradeoffs between risk and return in volatile market conditions. By implementing PSO, investors can potentially enhance portfolio performance, adapt quickly to changing market conditions, and achieve a higher degree of diversification with minimal computational effort (Laskari et al., 2002). The study highlights the mechanisms by which PSO achieves these outcomes, demonstrating its potential as a valuable tool in modern portfolio management.

2 Materials and Discussion

2.1 The Algorithm and Its Components

Particle Swarm Optimization (PSO) is a nature-inspired optimization algorithm that mimics the collective behavior observed in groups like flocks of birds, schools of fish, or swarms of insects. It is part of the broader category of swarm intelligence algorithms, which leverage decentralized, self-organized behaviors to solve complex problems.

At its core, PSO operates by creating a "swarm" of particles, where each particle represents a candidate solution in the problem's search space. The particles explore the search space by moving around, guided by both their individual experiences and the collective knowledge of the swarm. Each particle maintains two critical pieces of information: its personal best position (pBest)—the best solution it has found so far—and the global best position (gBest)—the best solution identified by the entire swarm at any given moment. Through this dual guidance mechanism, the particles collaborate, learning from their own success and the success of others, to converge toward an optimal or near-optimal solution.



Loc et al.; Asian J. Math. Comp. Res., vol. 32, no. 1, pp. 27-35, 2025; Article no.AJOMCOR.12616

Fig. 1. Particle Swarm Optimization Flow chart

2.2 Application in optimal asset allocation

Applying Particle Swarm Optimization (PSO) to optimal asset allocation requires defining each particle as a unique asset allocation across multiple investment options. In this application, PSO's components are tailored to search for an optimal mix of assets that meets specific investment goals, balancing expected returns and acceptable risk levels. The process unfolds as follows:

Initialization: At the outset, each particle is initialized with a random position, representing a specific asset allocation. In a typical asset allocation problem, these particles symbolize portfolios distributed across various asset classes, each with distinct characteristics and roles within a portfolio. Stocks represent equities that offer the potential for higher returns but are accompanied by higher risks, making them a key component for growth-oriented strategies. Bonds, on the other hand, are known for their lower risk and stable returns, adding balance and reducing overall portfolio volatility. Real estate provides diversification benefits along with potential income through rental yields, while commodities, such as gold or oil, act as a hedge against inflation and diversify the portfolio away from traditional asset classes like stocks and bonds.

Each particle's position in the search space is unique, showcasing a distinct proportion of these assets. For example, one particle might represent a portfolio with 40% in stocks, 30% in bonds, 20% in real estate, and 10% in commodities, while another might allocate 50% to bonds, 25% to stocks, 15% to real estate, and 10% to commodities. These randomized initial allocations ensure a broad coverage of the search space, enabling the algorithm to begin its exploration from a diverse set of starting points. This diversity is essential for uncovering optimal portfolio allocations, as it allows the particles to explore multiple paths toward achieving the best balance of risk and return.

Fitness Evaluation: The fitness function plays a critical role in evaluating each particle's portfolio allocation, measuring how effectively it aligns with the investor's objectives. This assessment is based on several key criteria that reflect the fundamental goals of portfolio optimization. Maximizing expected returns is one such criterion, where the fitness function estimates potential future returns using historical data or predictive models for each asset class. Portfolios with higher projected returns are rewarded, encouraging particles to prioritize allocations with greater profitability potential (Den Broeder et al., 1959).

Another essential criterion is minimizing risk, which involves quantifying the portfolio's volatility or downside risk using metrics such as standard deviation or Value at Risk (VaR). The function penalizes portfolios that exhibit excessive risk, guiding particles toward safer allocations that align with the investor's risk tolerance.

To address the trade-off between risk and return, the fitness function may also incorporate a combined objective using risk-adjusted return metrics like the Sharpe Ratio. This approach rewards portfolios that achieve higher returns per unit of risk, ensuring an optimized balance along the risk-return spectrum. By integrating these metrics, the fitness function evaluates the portfolio's efficiency, offering a comprehensive measure of its performance.

The resulting fitness score serves as a guiding signal for each particle, quantifying how close its current allocation is to the ideal balance of risk and return. This continuous feedback mechanism drives the swarm's collective progress, ultimately converging on the optimal portfolio allocation (Laskari et al., 2002).



Fig. 2. Particles' swarm searching for the global minimum of a function

A particle swarm searching for the global minimum of a function

Velocity and Position Updates:

Particles update their position and velocity based on both individual and collective learning mechanisms:

- a) **Personal Best (pBest)**: Each particle stores the best asset allocation it has achieved so far. If a particle finds an allocation that offers a better fitness score than its current best, it updates its personal best.
- b) **Global Best (gBest)**: The best allocation discovered by any particle in the swarm is stored as the global best. This value serves as a benchmark, guiding all particles toward a promising solution.
- c) **Velocity Update**: In each iteration, the algorithm calculates the particle's new velocity based on a combination of:
 - Inertia: The current velocity, which maintains some momentum in its previous direction.
 - Cognitive Component: The particle's tendency to return to its personal best.
 - **Social Component**: The particle's attraction toward the global best position, influenced by the rest of the swarm.

These velocity and position updates allow particles to explore a range of portfolio combinations, balancing exploration (searching new areas) and exploitation (refining known good solutions).

Particle Swarm Optimization For Optimal Asset Allocation

```
1. startTime <- Now
```

- 2. endTime <- startTime + allowedSearchTime
- 3. optimalPortfolio.allocations <- {}
- 4. optimalPortfolio.value <- MaxValue
- 5. swarm <- GenerateInitialSwarm(noOfParticles)
- 6. while Now < endTime do
- 7. *i* <- 1
- 8. while $i \le noOfParticles do$
- 9. swarm[i].portfolioValue <- CalculatePortfolioValue(swarm[i].allocations)
- 10. if swarm[i].portfolioValue == optimalPortfolio.value then
- 11. swarm[i].velocities <- GetRandomVelocities()
- 12. else
- 13. if swarm[i].portfolioValue > swarm[i].bestPortfolioValue then
- 14. swarm[i].bestPortfolioValue <- swarm[i].portfolioValue
- 15. swarm[i].bestAllocations <- swarm[i].allocations
- 16. if swarm[i].portfolioValue > optimalPortfolio.value then
- 17. optimalPortfolio.allocations <- swarm[i].allocations
- 18. optimalPortfolio.value <- swarm[i].portfolioValue
- 19. end if
- 20. end if
- 21. end if
- 22. i < -i + 1
- 23. end while
- 24. *i* <- 1
- 25. while $i \le noOfParticles$ do
- 26. *k* <- 1
- 27. while $k \le noOfAssets$ do
- 28. *swarm[i].velocities[k] <- UpdateVelocity(swarm[i], k)*
- 29. swarm[i].allocations[k] <- UpdatePosition(swarm[i], k)
- *30.* k < -k + 1
- 31. end while
- 32. i < -i + 1
- 33. end while
- 34. end while
- 35. return optimalPortfolio

Convergence: Over multiple iterations, particles adjust their allocations, gradually converging toward the optimal asset mix. The convergence process is critical for PSO as it helps particles focus on promising regions in the search space and avoid getting trapped in suboptimal allocations. By refining asset allocations through iterative adjustments, PSO identifies a balanced portfolio that aligns with the investor's risk-return preferences.

The end result is an efficient frontier for asset allocation, providing a range of portfolios that optimize the tradeoff between risk and return. By selecting from portfolios along this frontier, investors can choose a mix of assets tailored to their risk tolerance and financial objectives.



The optimization process of particle swarm optimization.

Fig. 3. The optimization process of particle swarm optimization

Advantages of PSO in Asset Allocation: PSO's iterative learning structure is particularly well-suited to navigating the large, complex search space of asset allocation. In contrast to traditional optimization techniques, which may struggle with nonlinearity and high dimensionality, PSO:

- Adapts to changing market conditions by continuously updating based on both individual and group performance.
- Provides flexibility in balancing risk and return, helping investors dynamically adjust their portfolios as the financial landscape evolves.

PSO's ability to efficiently explore and refine portfolio combinations makes it a powerful tool for achieving optimized asset allocations that align with investment goals.



Fig. 4. Effectiveness of PSO

3 Benefits, Future Potential, and Problem-Solving Ability

The application of Particle Swarm Optimization (PSO) in optimal asset allocation brings numerous advantages, both in its current capabilities and its potential for future development. By addressing the complexities of financial markets, PSO provides a robust and efficient approach to portfolio management, making it a valuable tool for investors.

3.1 Benefits of PSO in asset allocation

Computational Efficiency: Particle Swarm Optimization (PSO) demonstrates remarkable computational efficiency compared to traditional optimization techniques such as gradient descent or genetic algorithms. This efficiency stems from its ability to explore the search space simultaneously using multiple particles, which significantly reduces the time required to converge on an optimal solution. One key advantage is parallel exploration, where numerous particles work concurrently to investigate diverse portfolio allocations, accelerating the optimization process. Furthermore, PSO minimizes computational complexity by relying on straightforward position and velocity updates, avoiding the need for intricate derivative calculations or matrix operations. This reduction in overhead makes the algorithm lightweight and effective. Finally, PSO is highly time-sensitive, a critical attribute for financial markets that often demand rapid decision-making. By quickly identifying near-optimal asset allocations, PSO enables investors to adapt promptly to dynamic market conditions, ensuring efficiency and relevance in portfolio optimization.

Adaptability: PSO's swarm-based structure offers exceptional adaptability, allowing it to dynamically adjust to new market information or evolving investment objectives. One of its standout features is its ability to perform real-time adjustments, recalibrating asset allocations as new data emerges—whether it involves changes in asset performance, shifts in risk profiles, or updates to investor preferences. This flexibility ensures that portfolios remain aligned with current market conditions. Additionally, PSO excels at diverse portfolio exploration, balancing global and local searches to avoid premature convergence on suboptimal solutions while effectively responding to unforeseen market dynamics. Moreover, the algorithm offers customizable parameters, enabling investors to fine-tune key variables such as inertia and learning coefficients. This adaptability allows PSO to be tailored to specific financial scenarios, making it a versatile and powerful tool for navigating the complexities of asset allocation.

Improved Risk-Return Optimization: PSO excels at balancing the trade-off between risk and return, making it an invaluable tool for optimizing investment portfolios. Its ability to match risk tolerance is a key advantage, achieved by incorporating risk metrics such as standard deviation, Value at Risk (VaR), or Conditional VaR (CVaR) into its fitness function. This allows the algorithm to generate solutions that align with an investor's specific risk appetite. Additionally, PSO is highly effective at maximizing returns, actively seeking portfolio allocations that offer the highest potential returns while adhering to constraints like diversification rules and liquidity requirements. Another standout feature is PSO's ability to identify the efficient frontier, which represents a range of optimal portfolios balancing risk and return. This capability empowers investors to choose portfolios that best align with their individual financial goals, ensuring a customized and efficient approach to portfolio management.

3.2 Future potential of PSO in finance

Broader Applications: PSO's versatility extends beyond asset allocation, making it a valuable tool for various other financial applications. In algorithmic trading, PSO can optimize trading strategies by identifying the best parameter sets for generating buy/sell signals or implementing effective risk management rules. This ensures that trading systems remain adaptive and efficient in fast-paced markets. Additionally, PSO proves highly effective in portfolio rebalancing, dynamically adjusting asset allocations to maintain the desired proportions as market conditions change or as assets deviate from their original weights. This capability supports investors in sustaining their investment strategies over time. Furthermore, PSO is well-suited to derivatives pricing, solving complex mathematical models for options, swaps, and other financial instruments. By navigating the high-dimensional search spaces inherent in these problems, PSO delivers accurate and computationally efficient solutions, reinforcing its role as a versatile and powerful tool in modern finance (Holland, 1975; Dorigo, 1992).

Hybrid Models: Future developments in PSO hold immense potential, particularly through integration with other optimization and machine learning techniques to further enhance its performance. One promising direction is the development of hybrid PSO models, which combine the strengths of PSO with other methods such as genetic algorithms, simulated annealing, or reinforcement learning. These hybrids can address challenges like premature convergence or slow progress in large, complex search spaces, resulting in more robust and efficient optimization.

Another avenue for advancement is machine learning integration, where predictive models guide PSO's search process. By incorporating insights from historical data and market forecasts, PSO can adapt its exploration strategies to align with emerging trends, improving its ability to identify optimal solutions in dynamic environments. Additionally, the adoption of multi-objective PSO offers exciting possibilities. This approach extends the algorithm to handle multiple conflicting objectives simultaneously, such as maximizing returns, minimizing risk, and achieving environmental, social, and governance (ESG) compliance. These advancements not only broaden PSO's application scope but also enhance its relevance in tackling complex, real-world financial problems.

Improved Convergence and Robustness: Advancements in PSO could also focus on refining its parameter tuning and improving its robustness in challenging scenarios. Advanced parameter tuning techniques, such as adaptive inertia weights or self-tuning coefficients, offer the potential to enhance both the convergence speed and the accuracy of solutions. By dynamically adjusting these parameters during the optimization process, the algorithm becomes more responsive to the nuances of the search space, ensuring more precise results.

To address the complexity of modern financial markets, handling high dimensionality is another critical development. Enhanced PSO models could effectively manage large, intricate portfolios with hundreds of assets by leveraging dimensionality reduction techniques or clustering methods. These approaches simplify the search space, allowing PSO to maintain efficiency while tackling high-dimensional optimization problems (Blum & Roli, 2003).

Moreover, improving PSO's resilience in volatile markets is essential for its continued success in finance. By simulating diverse market conditions during training, PSO can learn to navigate unpredictable environments and deliver stable performance even during financial crises or periods of extreme volatility. These improvements ensure that PSO remains a reliable and versatile tool for portfolio management and other complex financial applications.

4 Conclusion and Future Scenarios

SO's inherent flexibility and swarm intelligence make it particularly adept at addressing emerging challenges in the ever-evolving financial landscape. Its stochastic nature equips it to navigate volatility and uncertainty effectively, enabling the algorithm to identify optimal solutions even in highly unpredictable market conditions. This resilience is especially valuable in times of economic turbulence or rapid market shifts (Laskari et al., 2002).

In the era of high-frequency data, PSO demonstrates its capability to handle the growing granularity of financial information. By processing vast amounts of real-time data, PSO can optimize portfolios or refine trading strategies with precision and speed, ensuring that investors remain competitive in fast-paced markets.

Additionally, PSO is well-positioned to support the growing emphasis on sustainability and ESG goals. By integrating environmental, social, and governance (ESG) metrics into its fitness function, the algorithm enables investors to construct portfolios that align with ethical and environmental priorities, without compromising on financial returns (Ihsan et al., 2021).

As financial markets become more complex, PSO's adaptability, computational efficiency, and problem-solving capacity solidify its role as a cornerstone of modern portfolio management (Hassan et al., 2005). Its ability to evolve in tandem with technological advancements and shifting market demands ensures its relevance and effectiveness in meeting the challenges of the future (Zlochin et al., 2004; Kennedy & Eberhart, 1995).

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Competing Interests

Authors have declared that no competing interests exist.

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